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### 1. Find

$$\int \left( 6x^2 + \frac{2}{x^2} + 5 \right) dx$$

giving each term in its simplest form.

(4)

Q1

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(Total 4 marks)



2. (a) Evaluate  $(32)^{\frac{3}{5}}$ , giving your answer as an integer.

(2)

(b) Simplify fully  $\left(\frac{25x^4}{4}\right)^{-\frac{1}{2}}$

(2)

Q2

(Total 4 marks)



P 4 0 6 8 4 A 0 3 2 4

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3. Show that  $\frac{2}{\sqrt{(12)} - \sqrt{(8)}}$  can be written in the form  $\sqrt{a} + \sqrt{b}$ , where  $a$  and  $b$  are integers. (5)



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### **Question 3 continued**

Q3

(Total 5 marks)



P 4 0 6 8 4 A 0 5 2 4

4.

$$y = 5x^3 - 6x^{\frac{4}{3}} + 2x - 3$$

- (a) Find  $\frac{dy}{dx}$  giving each term in its simplest form. (4)

(b) Find  $\frac{d^2y}{dx^2}$  (2)



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### **Question 4 continued**

Q4

(Total 6 marks)



P 4 0 6 8 4 A 0 7 2 4

5. A sequence of numbers  $a_1, a_2, a_3 \dots$  is defined by

$$a_1 = 3$$

$$a_{n+1} = 2a_n - c \quad (n \geq 1)$$

where  $c$  is a constant.

- (a) Write down an expression, in terms of  $c$ , for  $a_2$

(1)

- (b) Show that  $a_3 = 12 - 3c$

(2)

Given that  $\sum_{i=1}^4 a_i \geq 23$

(4)



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### **Question 5 continued**

Q5

(Total 7 marks)



P 4 0 6 8 4 A 0 9 2 4

6. A boy saves some money over a period of 60 weeks. He saves 10p in week 1, 15p in week 2, 20p in week 3 and so on until week 60. His weekly savings form an arithmetic sequence.

- (a) Find how much he saves in week 15 (2)

- (b) Calculate the total amount he saves over the 60 week period. (3)

The boy's sister also saves some money each week over a period of  $m$  weeks. She saves 10p in week 1, 20p in week 2, 30p in week 3 and so on so that her weekly savings form an arithmetic sequence. She saves a total of £63 in the  $m$  weeks.

- (c) Show that

$$m(m+1) = 35 \times 36 \quad (4)$$

- (d) Hence write down the value of  $m$ . (1)



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### **Question 6 continued**



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## **Question 6 continued**



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## **Question 6 continued**

Q6

(Total 10 marks)



7. The point  $P(4, -1)$  lies on the curve  $C$  with equation  $y = f(x)$ ,  $x > 0$ , and

$$f'(x) = \frac{1}{2}x - \frac{6}{\sqrt{x}} + 3$$

- (a) Find the equation of the tangent to  $C$  at the point  $P$ , giving your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are integers.

(4)

- (b) Find  $f(x)$ .

(4)



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### **Question 7 continued**

Q7

(Total 8 marks)



**8.**  $4x - 5 - x^2 = q - (x + p)^2$

where  $p$  and  $q$  are integers.

- (a) Find the value of  $p$  and the value of  $q$ . (3)

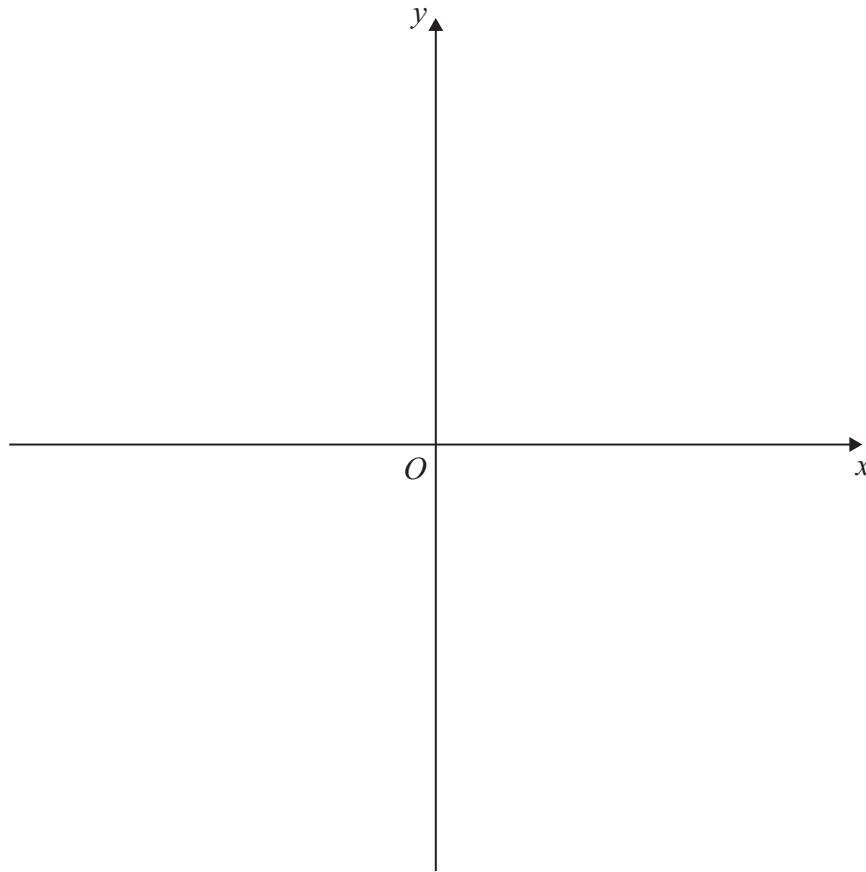
(b) Calculate the discriminant of  $4x - 5 - x^2$  (2)

(c) On the axes on page 17, sketch the curve with equation  $y = 4x - 5 - x^2$  showing clearly the coordinates of any points where the curve crosses the coordinate axes. (3)



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**Question 8 continued**



Q8

(Total 8 marks)



9. The line  $L_1$  has equation  $4y + 3 = 2x$

The point  $A(p, 4)$  lies on  $L_1$

- (a) Find the value of the constant  $p$ .

(1)

The line  $L_2$  passes through the point  $C(2, 4)$  and is perpendicular to  $L_1$ .

- (b) Find an equation for  $L_2$  giving your answer in the form  $ax + by + c = 0$ , where  $a, b$  and  $c$  are integers.

(5)

The line  $L_1$  and the line  $L_2$  intersect at the point  $D$ .

- (c) Find the coordinates of the point  $D$ .

(3)

- (d) Show that the length of  $CD$  is  $\frac{3}{2}\sqrt{5}$

(3)

A point  $B$  lies on  $L_1$  and the length of  $AB = \sqrt{80}$

The point  $E$  lies on  $L_2$  such that the length of the line  $CDE = 3$  times the length of  $CD$ .

- (e) Find the area of the quadrilateral  $ACBE$ .

(3)



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**Question 9 continued**



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**Question 9 continued**



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## **Question 9 continued**

Q9

(Total 15 marks)



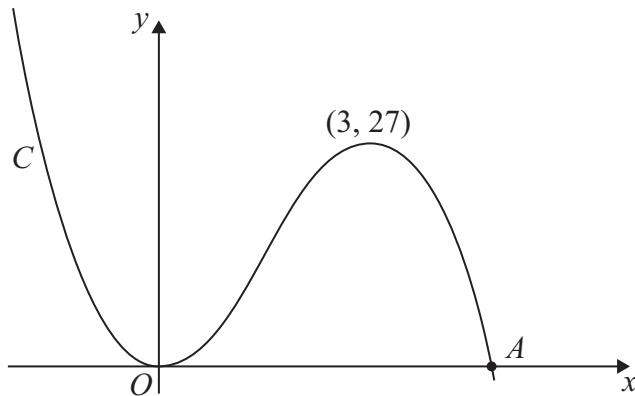
**10.****Figure 1**

Figure 1 shows a sketch of the curve  $C$  with equation  $y = f(x)$  where

$$f(x) = x^2(9 - 2x)$$

There is a minimum at the origin, a maximum at the point  $(3, 27)$  and  $C$  cuts the  $x$ -axis at the point  $A$ .

- (a) Write down the coordinates of the point  $A$ .

(1)

- (b) On separate diagrams sketch the curve with equation

(i)  $y = f(x + 3)$

(ii)  $y = f(3x)$

On each sketch you should indicate clearly the coordinates of the maximum point and any points where the curves cross or meet the coordinate axes.

(6)

The curve with equation  $y = f(x) + k$ , where  $k$  is a constant, has a maximum point at  $(3, 10)$ .

- (c) Write down the value of  $k$ .

(1)

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**Question 10 continued**



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**Question 10 continued**

Q10

(Total 8 marks)

**TOTAL FOR PAPER: 75 MARKS**

**END**

