Centre No.							Paper Reference						Surname		Initial(s)
Candidate No.						**6**	**6**	**8**	**3**	**/**	**0**	**1**	Signature		

Edexcel GCE

Statistics S1

Advanced/Advanced Subsidiary

Tuesday 16 January 2007 – Morning

Time: 1 hour 30 minutes

Materials required for examination   **Items included with question papers**
Mathematical Formulae (Green)   Nil

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration. Thus candidates may NOT use calculators such as the Texas Instruments TI 89, TI 92, Casio CFX 9970G, Hewlett Packard HP 48G.

Examiner's use only		

Team Leader's use only		

Question Number	Leave Blank
1	
2	
3	
4	
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6	
7	
Total	

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initial(s) and signature.
Check that you have the correct question paper.
You must write your answer for each question in the space following the question.
Values from the statistical tables should be quoted in full. When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.
Full marks may be obtained for answers to ALL questions.
The marks for individual questions and parts of questions are shown in round brackets: e.g. **(2)**.
There are 7 questions in this question paper. The total for this question paper is 75.
There are 20 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.
You must show sufficient working to make your methods clear to the examiner. Answers without working may gain no credit.

Turn over

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1. As part of a statistics project, Gill collected data relating to the length of time, to the nearest minute, spent by shoppers in a supermarket and the amount of money they spent. Her data for a random sample of 10 shoppers are summarised in the table below, where t represents time and £m the amount spent over £20.

t (minutes)	£m
15	−3
23	17
5	−19
16	4
30	12
6	−9
32	27
23	6
35	20
27	6

(a) Write down the actual amount spent by the shopper who was in the supermarket for 15 minutes.

(1)

(b) Calculate S_{tt}, S_{mm} and S_{tm}.

(You may use $\Sigma t^2 = 5478$ $\Sigma m^2 = 2101$ $\Sigma tm = 2485$)

(6)

(c) Calculate the value of the product moment correlation coefficient between t and m.

(3)

(d) Write down the value of the product moment correlation coefficient between t and the actual amount spent. Give a reason to justify your value.

(2)

On another day Gill collected similar data. For these data the product moment correlation coefficient was 0.178

(e) Give an interpretation to both of these coefficients.

(2)

(f) Suggest a practical reason why these two values are so different.

(1)

Question 1 continued

Question 1 continued

N 2 3 9 5 7 A 0 4 2 0

Question 1 continued

(Total 15 marks)

Q1

2. In a factory, machines A, B and C are all producing metal rods of the same length. Machine A produces 35% of the rods, machine B produces 25% and the rest are produced by machine C. Of their production of rods, machines A, B and C produce 3%, 6% and 5% defective rods respectively.

(a) Draw a tree diagram to represent this information.

(3)

(b) Find the probability that a randomly selected rod is

    (i) produced by machine A and is defective,

    (ii) is defective.

(5)

(c) Given that a randomly selected rod is defective, find the probability that it was produced by machine C.

(3)

Question 2 continued

(Total 11 marks)

Q2

N 2 3 9 5 7 A 0 7 2 0

3. The random variable X has probability function

$$P(X = x) = \frac{(2x - 1)}{36} \qquad x = 1, 2, 3, 4, 5, 6.$$

(a) Construct a table giving the probability distribution of X.

(3)

Find

(b) $P(2 < X \leqslant 5)$,

(2)

(c) the exact value of $E(X)$.

(2)

(d) Show that $Var(X) = 1.97$ to 3 significant figures.

(4)

(e) Find $Var(2 - 3X)$.

(2)

Question 3 continued

(Total 13 marks)

Q3

4. Summarised below are the distances, to the nearest mile, travelled to work by a random sample of 120 commuters.

Distance (to the nearest mile)	Number of commuters
0–9	10
10–19	19
20–29	43
30–39	25
40–49	8
50–59	6
60–69	5
70–79	3
80–89	1

For this distribution,

(a) describe its shape,

(1)

(b) use linear interpolation to estimate its median.

(2)

The mid-point of each class was represented by x and its corresponding frequency by f giving

$$\Sigma fx = 3550 \quad \text{and} \quad \Sigma fx^2 = 138020$$

(c) Estimate the mean and the standard deviation of this distribution.

(3)

One coefficient of skewness is given by

$$\frac{3(\text{mean} - \text{median})}{\text{standard deviation}}.$$

(d) Evaluate this coefficient for this distribution.

(3)

(e) State whether or not the value of your coefficient is consistent with your description in part (a). Justify your answer.

(2)

(f) State, with a reason, whether you should use the mean or the median to represent the data in this distribution.

(2)

(g) State the circumstance under which it would not matter whether you used the mean or the median to represent a set of data.

(1)

Question 4 continued

Question 4 continued

(Total 14 marks)

Q4

N 2 3 9 5 7 A 0 1 3 2 0

5. A teacher recorded, to the nearest hour, the time spent watching television during a particular week by each child in a random sample. The times were summarised in a grouped frequency table and represented by a histogram.

One of the classes in the grouped frequency distribution was 20–29 and its associated frequency was 9. On the histogram the height of the rectangle representing that class was 3.6 cm and the width was 2 cm.

(a) Give a reason to support the use of a histogram to represent these data.

(1)

(b) Write down the underlying feature associated with each of the bars in a histogram.

(1)

(c) Show that on this histogram each child was represented by $0.8 \, \text{cm}^2$.

(3)

The total area under the histogram was $24 \, \text{cm}^2$.

(d) Find the total number of children in the group.

(2)

Question 5 continued

(Total 7 marks)

Q5

N 2 3 9 5 7 A 0 1 5 2 0

6. (a) Give two reasons to justify the use of statistical models.

(2)

It has been suggested that there are 7 stages involved in creating a statistical model. They are summarised below, with stages 3, 4 and 7 missing.

Stage 1. The recognition of a real-world problem.

Stage 2. A statistical model is devised.

Stage 3.

Stage 4.

Stage 5. Comparisons are made against the devised model.

Stage 6. Statistical concepts are used to test how well the model describes the real-world problem.

Stage 7.

(b) Write down the missing stages.

(3)

Question 6 continued

7. The measure of intelligence, IQ, of a group of students is assumed to be Normally distributed with mean 100 and standard deviation 15.

   (a) Find the probability that a student selected at random has an IQ less than 91.

   (4)

   The probability that a randomly selected student has an IQ of at least $100 + k$ is 0.2090.

   (b) Find, to the nearest integer, the value of k.

   (6)

Question 7 continued

Q7

(Total 10 marks)

TOTAL FOR PAPER: 75 MARKS

END

N 2 3 9 5 7 A 0 1 9 2 0

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