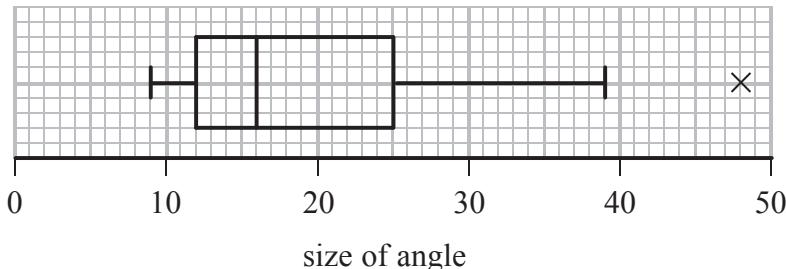


1. Each of 60 students was asked to draw a 20° angle without using a protractor. The size of each angle drawn was measured. The results are summarised in the box plot below.



- (a) Find the range for these data. (1)
- (b) Find the interquartile range for these data. (1)

The students were then asked to draw a 70° angle.

The results are summarised in the table below.

Angle, a , (degrees)	Number of students
$55 \leq a < 60$	6
$60 \leq a < 65$	15
$65 \leq a < 70$	13
$70 \leq a < 75$	11
$75 \leq a < 80$	8
$80 \leq a < 85$	7

- (c) Use linear interpolation to estimate the size of the median angle drawn. Give your answer to 1 decimal place. (2)

- (d) Show that the lower quartile is 63° (2)

For these data, the upper quartile is 75° , the minimum is 55° and the maximum is 84°

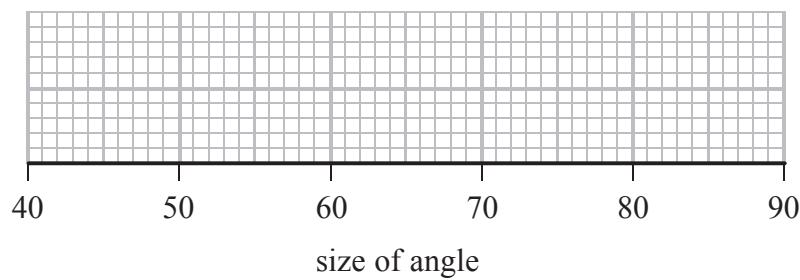
An outlier is an observation that falls either more than $1.5 \times (\text{interquartile range})$ above the upper quartile or more than $1.5 \times (\text{interquartile range})$ below the lower quartile.

- (e) (i) Show that there are no outliers for these data.
(ii) Draw a box plot for these data on the grid on page 3. (5)
- (f) State which angle the students were more accurate at drawing. Give reasons for your answer. (3)



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Question 1 continued



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Question 1 continued



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Question 1 continued

Q1

(Total 14 marks)



2. An estate agent recorded the price per square metre, p £/m², for 7 two-bedroom houses.

He then coded the data using the coding $q = \frac{p - a}{b}$, where a and b are positive constants.

His results are shown in the table below.

p	1840	1848	1830	1824	1819	1834	1850
q	4.0	4.8	3.0	2.4	1.9	3.4	5.0

- (a) Find the value of a and the value of b

(2)

The estate agent also recorded the distance, d km, of each house from the nearest train station. The results are summarised below.

$$S_{dd} = 1.02 \quad S_{qq} = 8.22 \quad S_{dq} = -2.17$$

- (b) Calculate the product moment correlation coefficient between d and q

(2)

- (c) Write down the value of the product moment correlation coefficient between d and p

(1)

The estate agent records the price and size of 2 additional two-bedroom houses, H and J .

House	Price (£)	Size (m ²)
H	156 400	85
J	172 900	95

- (d) Suggest which house is most likely to be closer to a train station. Justify your answer.

(3)



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Question 2 continued



P 4 4 8 4 5 A 0 7 2 4

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Question 2 continued



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Question 2 continued

Q2

(Total 8 marks)



P 4 4 8 4 5 A 0 9 2 4

3. A college has 80 students in Year 12.

20 students study Biology
28 students study Chemistry
30 students study Physics
7 students study both Biology and Chemistry
11 students study both Chemistry and Physics
5 students study both Physics and Biology
3 students study all 3 of these subjects

- (a) Draw a Venn diagram to represent this information.

(5)

A Year 12 student at the college is selected at random.

- (b) Find the probability that the student studies Chemistry but not Biology or Physics.

(1)

- (c) Find the probability that the student studies Chemistry or Physics or both.

(2)

Given that the student studies Chemistry or Physics or both,

- (d) find the probability that the student does not study Biology.

(2)

- (e) Determine whether studying Biology and studying Chemistry are statistically independent.

(3)



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Question 3 continued



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Question 3 continued



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Question 3 continued

Q3

(Total 13 marks)



P 4 4 8 4 5 A 0 1 3 2 4

4. Statistical models can provide a cheap and quick way to describe a real world situation.

- (a) Give two other reasons why statistical models are used.

(2)

A scientist wants to develop a model to describe the relationship between the average daily temperature, x °C, and her household's daily energy consumption, y kWh, in winter.

A random sample of the average daily temperature and her household's daily energy consumption are taken from 10 winter days and shown in the table.

x	-0.4	-0.2	0.3	0.8	1.1	1.4	1.8	2.1	2.5	2.6
y	28	30	26	25	26	27	26	24	22	21

[You may use $\sum x^2 = 24.76$ $\sum y = 255$ $\sum xy = 283.8$ $S_{xx} = 10.36$]

- (b) Find S_{xy} for these data.

(3)

- (c) Find the equation of the regression line of y on x in the form $y = a + bx$

Give the value of a and the value of b to 3 significant figures.

(4)

- (d) Give an interpretation of the value of a

(1)

- (e) Estimate her household's daily energy consumption when the average daily temperature is 2 °C

(2)

The scientist wants to use the linear regression model to predict her household's energy consumption in the summer.

- (f) Discuss the reliability of using this model to predict her household's energy consumption in the summer.

(2)



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Question 4 continued



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Question 4 continued



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Question 4 continued

Q4

(Total 14 marks)



5. In a quiz, a team gains 10 points for every question it answers correctly and loses 5 points for every question it does not answer correctly. The probability of answering a question correctly is 0.6 for each question. One round of the quiz consists of 3 questions.

The discrete random variable X represents the total number of points scored in one round. The table shows the incomplete probability distribution of X

x	30	15	0	-15
$P(X=x)$	0.216			0.064

- (a) Show that the probability of scoring 15 points in a round is 0.432 (2)
- (b) Find the probability of scoring 0 points in a round. (1)
- (c) Find the probability of scoring a total of 30 points in 2 rounds. (3)
- (d) Find $E(X)$ (2)
- (e) Find $\text{Var}(X)$ (3)
- In a bonus round of 3 questions, a team gains 20 points for every question it answers correctly and loses 5 points for every question it does not answer correctly.
- (f) Find the expected number of points scored in the bonus round. (3)
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Question 5 continued



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Question 5 continued



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Question 5 continued

Q5

(Total 14 marks)



- ## 6. The random variable $Z \sim N(0, 1)$

A is the event $Z > 1.1$

B is the event $Z > -1.9$

C is the event $-1.5 < Z < 1.5$

(a) Find

(i) $P(A)$

(ii) $P(B)$

(iii) P(C)

(iv) $P(A \cup C)$

(6)

The random variable X has a normal distribution with mean 21 and standard deviation 5

(b) Find the value of w such that $P(X > w \mid X > 28) = 0.625$

(6)



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Question 6 continued



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Question 6 continued

Q6

(Total 12 marks)

TOTAL FOR PAPER: 75 MARKS

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